

$$\lim_{x \rightarrow -\infty} (\sqrt{x^2 + x + 1} + x)$$

⚠ $x \rightarrow -\infty$ で $\infty - \infty$ 型の不定形

$$= \lim_{x \rightarrow -\infty} \frac{(\sqrt{x^2 + x + 1} + x)(\sqrt{x^2 + x + 1} - x)}{\sqrt{x^2 + x + 1} - x}$$

$$= \lim_{x \rightarrow -\infty} \frac{x + 1}{\sqrt{x^2 + x + 1} - x}$$

$$\lim_{x \rightarrow -\infty} (\sqrt{x^2 + x + 1} + x) = \lim_{x \rightarrow -\infty} \frac{x + 1}{\sqrt{x^2 + x + 1} - x}$$

$$= \lim_{x \rightarrow -\infty} \frac{\frac{1}{-x}(x + 1)}{\frac{1}{-x}(\sqrt{x^2 + x + 1} - x)}$$

$$= \lim_{x \rightarrow -\infty} \frac{-1 - \frac{1}{x}}{\sqrt{1 + \frac{1}{x} + \frac{1}{x^2}} + 1} = -\frac{1}{2}$$

$$\triangle! \ x < 0 \text{ より } \frac{1}{-x}\sqrt{x^2 + x + 1} = \sqrt{\frac{x^2 + x + 1}{(-x)^2}}$$