

$$\begin{aligned}(1) \quad (xe^{2x})^{(n)} &= (e^{2x}x)^{(n)} \\&= (e^{2x})^{(n)}x + {}_nC_1(e^{2x})^{(n-1)}x' + \cdots + e^{2x}x^{(n)} \\&= (e^{2x})^{(n)}x + {}_nC_1(e^{2x})^{(n-1)}x' \\&= 2^n xe^{2x} + n2^{n-1}e^{2x}\end{aligned}$$